



Secret Key (symmetric) Cryptography

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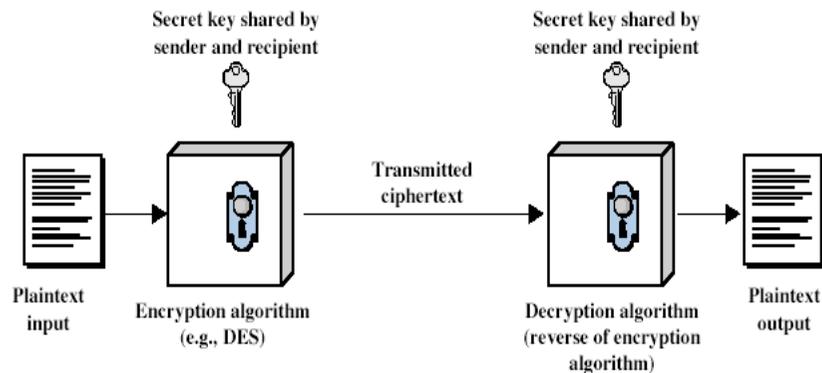
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<http://www.tlc.unipr.it/veltri>

Symmetric Encryption

- Or conventional / private-key / single-key
- Sender and recipient share a common key
- All classical encryption algorithms are private-key
- Was the only type prior to invention of public-key in 1970's
- Secret key cryptographic systems are designed to take a reasonable-length key (e.g. 64 bits) and generating a one-to-one mapping that "looks like completely **random**", to someone doesn't know the key

Symmetric Cipher Model



Symmetric Cipher Model

- two requirements for secure use of symmetric encryption:
 - a **strong encryption algorithm**
 - a **shared secret key known only to sender / receiver**
- plaintext = m
- ciphertext = $c = E_k(m)$
- decrypted plaintext = $D_k(c) = D_k(E_k(m)) = m$
- assume encryption algorithm is known
- implies a secure channel to distribute key

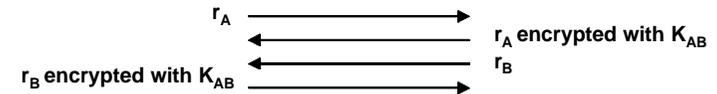
Symmetric Cipher Characteristics

- Richiede una fase iniziale in cui ciascuna coppia di interlocutori si scambia la secret key in maniera sicura
- Il numero delle chiavi per realizzare una comunicazione reciproca tra N utenti (dispositivi) è pari a $N \times (N-1) / 2$ (se le chiavi rimangono sempre le stesse)
- Viene generalmente utilizzato per proteggere, mediante codifica, informazioni (file) in un repository locale o trasmessi
- La robustezza dell'algoritmo è normalmente misurata dalla lunghezza delle chiavi: 40 bit (debole), 128 bit (forte)
- Algoritmi più diffusi: DES, 3DES, RC2, RC4, IDEA, AES

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Security uses of secret key cryptography

- Transmitting over an insecure channel
 - **the two parties agree on a shared secret key and use secret key cryptography to send messages**
- Secure storage on insecure media
 - **the user uses a secret key to store and retrieve data on an (insecure) media**
- Authentication
 - **strong authentication through a challenge-response mechanism**



- Integrity check
 - **generating a fixed-length cryptographic checksum associated with a message (Message Integrity Code - MIC)**

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Difetti dei sistemi simmetrici

- Metodo per scambio di chiavi assente
- Numero di chiavi troppo grande per gestire dei segreti condivisi tra singoli utenti
[$n(n-1) / 2$]

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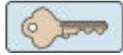
Classical Substitution Ciphers

- where letters of plaintext are replaced by other letters or by numbers or symbols
- or if plaintext is viewed as a sequence of bits, then substitution involves replacing plaintext bit patterns with ciphertext bit patterns

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Crittografia classica con sostituzione: esempi

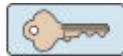
Cifrario con shift



Chiave $K \in \{0, 1, \dots, 25\}$

$$X_i \leftarrow M_i + K \pmod{26}$$

Cifrario monoalfabetico



Chiave

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
O	C	T	M	B	W	L	A	K	J	D	X	I	N	E	Y	S	U	P	F	Z	R	Q	H	V	G

testo in chiaro: C A S A

testo cifrato: T O P O

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Caesar Cipher

- earliest known substitution cipher
- by Julius Caesar
- first attested use in military affairs
- replaces each letter by 3rd letter on
- example:
meet me after the toga party
PHHW PH DIWHU WKH WRJD SDUWB

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Caesar Cipher (cont.)

- can define transformation as:
a b c d e f g h i j k l m n o p q r s t u v w x y z
D E F G H I J K L M N O P Q R S T U V W X Y Z A B C
- mathematically give each letter a number
a b c d e f g h i j k l m
0 1 2 3 4 5 6 7 8 9 10 11 12
n o p q r s t u v w x y z
13 14 15 16 17 18 19 20 21 22 23 24 25
- then have Caesar cipher as:
 $C = E(p) = (p + k) \pmod{26}$
 $p = D(C) = (C - k) \pmod{26}$

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Monoalphabetic Cipher

- rather than just shifting the alphabet
 - could shuffle (jumble) the letters arbitrarily
 - each plaintext letter maps to a different random ciphertext letter
 - hence key is 26 letters long
- Plain: abcdefghijklmnopqrstuvwxyz
Cipher: DKVQFIBJWPESCXHTMYAUOLRGZN
- Plaintext: ifwewishtoreplaceletters
Ciphertext: WIRFRWAJUHYFTSDVFSFUUFYA

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Monoalphabetic Cipher Security

- now have a total of $26! = 4 \times 10^{26}$ keys
- with so many keys, might think is secure
- but would be WRONG!!
- problem is language characteristics
 - letter frequencies
 - most common words
 - two letters frequencies (e.g. "th" in english)
 - etc.

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Polyalphabetic Ciphers

- another approach to improving security is to use multiple cipher alphabets
- called **polyalphabetic substitution ciphers**
- makes cryptanalysis harder with more alphabets to guess and flatter frequency distribution
- use a key to select which alphabet is used for each letter of the message
- use each alphabet in turn
- repeat from start after end of key is reached

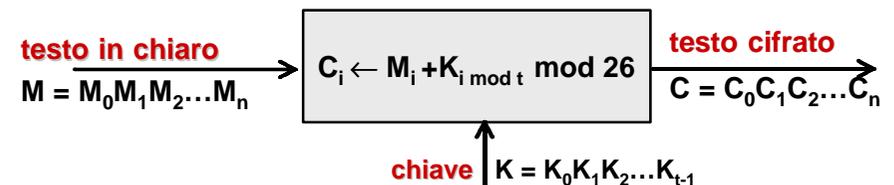
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Vigenère Cipher

- simplest polyalphabetic substitution cipher is the **Vigenère Cipher** [1586]
 - (Blaise de Vigenère, 1523-1596)
- effectively multiple caesar ciphers
- key is multiple letters long $K = k_1 k_2 \dots k_d$
- i^{th} letter specifies i^{th} alphabet to use
- use each alphabet in turn
- repeat from start after d letters in message
- decryption simply works in reverse

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Vigenère Cipher (cont.)



Esempio

Testo in chiaro: CODICE MOLTO SICURO

Chiave: REBUS

	CODIC	EMOLT	OSICU	RO	testo in
chiaro					
	REBUS	REBUS	REBUS	RE	chiave
	TSECU	VQPFL	FWJWM	IS	testo
cifrato					

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Cryptanalysis of Vigenère Ciphers

- have multiple ciphertext letters for each plaintext letter
- hence letter frequencies are obscured
- but not totally lost
- start with letter frequencies
 - see if look monoalphabetic or not
- if not, then need to determine number of alphabets, since then can attach each

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One-Time Pad

- if a truly random key as long as the message is used, the cipher will be secure
- called a One-Time pad
- Advantages:
 - is unbreakable since ciphertext bears no statistical relationship to the plaintext, and
 - for any plaintext & any ciphertext there exists a key mapping one to other
- Disadvantages:
 - can only use the key once
 - have problem of safe distribution of key

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Transposition Ciphers

- another technique is that used by classical **transposition** or **permutation** ciphers
- these hide the message by rearranging the letter order (blocks of bits)
- without altering the actual letters used
- can recognise these since have the same frequency distribution as the original text

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Example: Row Transposition Ciphers

- a more complex scheme
- write letters of message out in rows over a specified number of columns
- then reorder the columns according to some key before reading off the rows

```
Key:      4 3 1 2 5 6 7
Plaintext: a t t a c k p
           o s t p o n e
           d u n t i l t
           w o a m x y z
Ciphertext: TTNAAPTMTSUOAODWCOIXKNLYPETZ
```

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Product Ciphers

- Ciphers using substitutions or transpositions are not secure because of language characteristics
- Hence consider using several ciphers in succession to make harder:
 - **two substitutions make a more complex substitution**
 - **two transpositions make more complex transposition**
 - **but a substitution followed by a transposition makes a new much harder cipher**
- This is bridge from classical to modern ciphers

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Rotor Machines

- Before modern ciphers, rotor machines were most common product cipher
- Were widely used in WW2
 - **German Enigma, Allied Hagelin, Japanese Purple**
- Implemented a very complex, varying substitution cipher
- Used a series of cylinders, each giving one substitution, which rotated and changed after each letter was encrypted
- with 3 cylinders have $26 \times 26 \times 26 = 26^3 = 17576$ alphabets

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Steganography

- an alternative to encryption
- hides existence of message
 - **using only a subset of letters/words in a longer message marked in some way**
 - **using invisible ink**
 - **hiding in graphic image or sound file**
- has drawbacks
 - **high overhead to hide relatively few info bits**

Block and Stream Ciphers

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Block and Stream Ciphers

- There are two basic cipher structures
 - **Block ciphers**
 - Block ciphers process messages in into blocks, each of which is then en/decrypted
 - Plaintext is treated as a sequence of n-bit blocks of data
 - Ciphertext is same length as plaintext
 - Like a substitution on very big characters (64-bits or more)
 - Can be made to behave as a stream cipher
 - **Stream ciphers**
 - Stream ciphers process messages (Encryption/Decryption) a bit or byte at a time when en/decrypting
 - Often easier to analyze mathematically
- many current ciphers are block ciphers

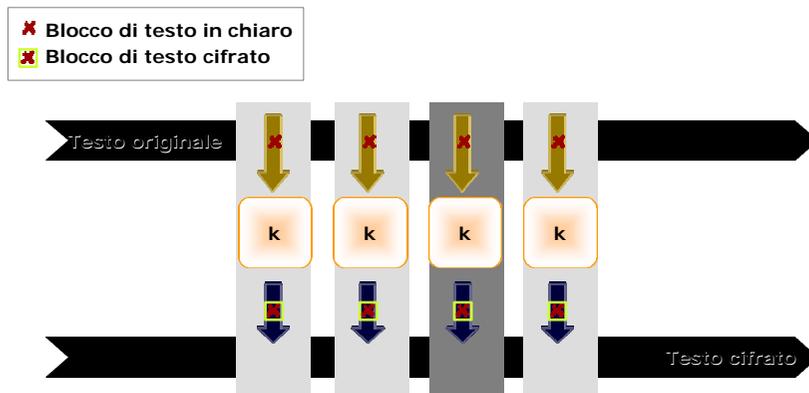
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Block Ciphers

- A cryptographic algorithm convert a plaintext block into an encrypted block
- How long should the plaintext block be?
 - **having block length too short (say one byte as in monoalphabetic cipher), it could be easier to construct a decryption table starting from some <plaintext,ciphertext> pairs**
 - **having block length too long, it could be inconvenient due to the increasing of complexity**
- 64bit blocks are often used
 - **it is difficult to obtain all 2^{64} pairs(known plaintext attack)..**

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Example of Block Ciphers



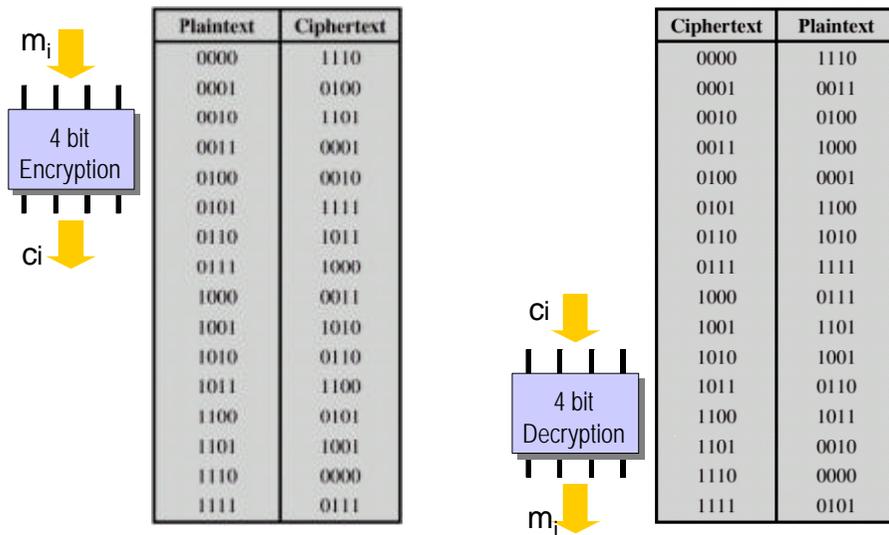
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Block Ciphers

- block ciphers look like an extremely large substitution
- If 64bit blocks are used, 2^{64} possible input values are mapped to 2^{64} output values
- The most general way of encrypting could be to specify completely the mapping table
 - would need table of 2^{64} entries for a 64-bit block $\rightarrow 2^{70}$ bits!
 - it is too long for a key.. ;-)
 - instead create from smaller building blocks

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Esempio di crittografia a blocchi di 4 bit



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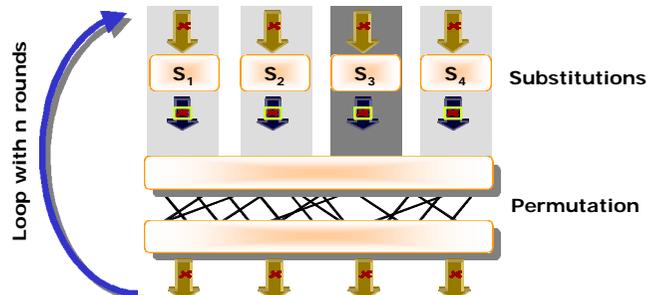
Block Ciphers

- Two kind of simple transformations are used:
 - **substitutions**
 - specifies for each of the 2^k possible input values the k -bit output
 - this is not practical for 64-bit blocks, but is possible for lower length blocks (e.g. 8bits)
 - to specify a substitution on k -bit blocks, $k \cdot 2^k$ bits are required
 - **permutations**
 - specifies for each of the k input bits the corresponding output position
 - a permutation is a special case of substitution in which each bit of the output gets its value from exactly one bit of the input
 - to specify a permutation on k -bit blocks, $k \cdot \log_2 k$ bits are required

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Block Ciphers

- One possible way to build a secret key algorithm is
 - to break the input into managed-sized chunks (say 8 bits),
 - do a substitution on each small chunk,
 - and then take the output of all the substitutions and run them through a permuter (big as the input)
 - the process is repeated, so that each bit winds up as input to each substitution
 - Each time is called *round*



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Substitution-Permutation Ciphers

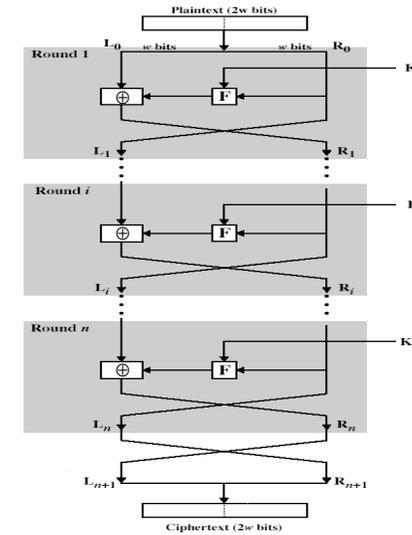
- Cipher needs to completely obscure statistical properties of original message
 - a **one-time pad** does this
- in 1949 Claude Shannon introduced idea of substitution-permutation (S-P) networks
- S-P networks are based on the two primitive cryptographic operations:
 - **substitution**
 - **permutation**
- these form the basis of modern block ciphers
- provide confusion and diffusion of message
 - **confusion**
 - makes relationship between ciphertext and key as complex as possible
 - **diffusion**
 - dissipates statistical structure of plaintext over bulk of ciphertext
 - every single plaintext cipher will influence several ciphertext ciphers
- the operation must be reversible!

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Feistel Cipher Structure

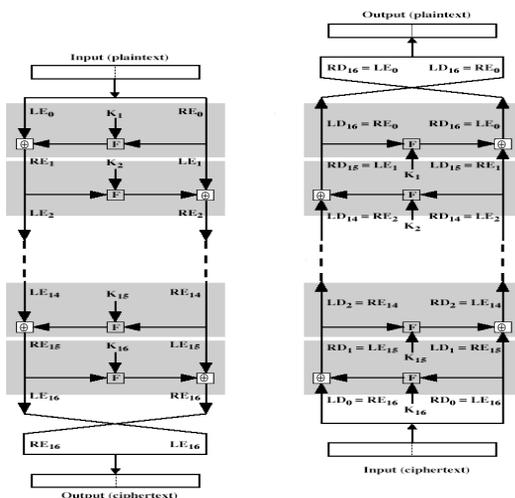
- Horst Feistel devised the **cipher** based on concept of invertible product cipher
 - - process through multiple rounds which perform a substitution on left data half
 - then have permutation swapping halves
- implements Shannon's substitution-permutation network concept

Feistel Cipher Structure



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Feistel Cipher Decryption



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Design Principles

Block Ciphers are defined in terms of

- **block size**
 - increasing size improves security, but slows cipher
- **key size**
 - increasing size improves security, makes exhaustive key searching harder, but may slow cipher
- **number of rounds**
 - greater number improves security, but slows cipher
- **subkey generation**
 - greater complexity can make analysis harder, but slows cipher
- **round function**
 - greater complexity can make analysis harder, but slows cipher

Two other considerations

- **fast software en/decryption & ease of analysis**
 - are more recent concerns for practical use and testing

Data Encryption Standard (DES)

- Most widely used block cipher in world
- Published in 1977 by National Bureau of Standards (now NIST) for use in commercial and unclassified U.S. Government applications
- FIPS PUB 46-3 (Federal Information Processing Standards PUBLication)
 - **U.S. Dept. OF Commerce/NIST (National Institute of Standards and Technology)**
- Has widespread use
- Has been considerable controversy over its security

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DES History

- Based on an algorithm known as *Lucifer cipher* (1971)
 - **by an IBM team led by Horst Feistel**
 - **used 64-bit data blocks with 128-bit key**
- then redeveloped as a commercial cipher with input from NSA and others
- in 1973 NBS issued request for proposals for a national cipher standard
- IBM submitted their revised Lucifer which was eventually accepted as the DES
- DES has become widely used, esp in financial applications
- in 1999 NIST published a new version called *triple DES* (3DES) or *TDEA*

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Data Encryption Standard (DES)

- DES encrypts 64-bit data using 56-bit key
- It consists of
 - **initial permutation of the 64 bits**
 - **16 identical "rounds" of operation where the data is confused and diffused with the key and the previous round**
 - **A final permutation**
- DES can be efficiently implemented in hardware
- Relatively slow if implemented in software
 - **this was not a documented goal**
 - **..however people have asserted that it was designed with this in mind**

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DES Design Controversy

- although DES standard is public
- was considerable controversy over design
 - in choice of 56-bit key (vs Lucifer 128-bit)
 - and because design criteria were classified
- subsequent events and public analysis show design was appropriate

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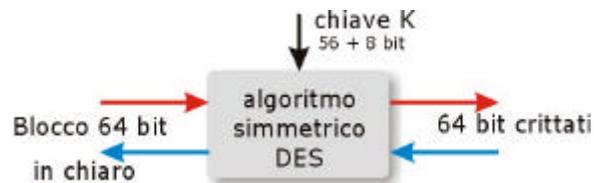
Why 56bits keys?

- yes.. 8x7 bits + 8 bits for parity check..
- however, 8 bits for parity check are too small
 - 64 bits of garbage have 1 in 256 chance to look like a valid key
- people have suggested that key length has been reduced from 64 to 56 to let DES to be broken (only) by the NSA (15 years ago..)

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DES

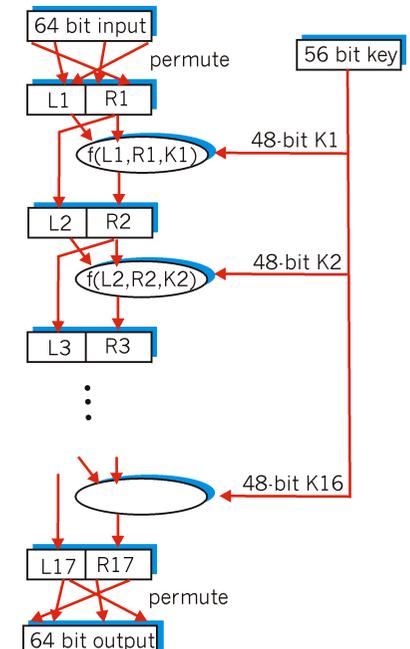
- Uses a 64-bit key that is reduced to 56-bits for parity checking
 - The 56-bit key is transformed in to 16 48-bit subkeys (one per round)
- Transforms 64-bit blocks of input M to 64-bit blocks of output C
- Same algorithm for encryption and decryption (sub-keys are used in reverse order for decryption)



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DES

- Consists of
 - An initial permutation (P)
 - Key transformation
 - 16 rounds of:
 - the rightmost 32 bits of the input are moved to the left 32 bits of the output
 - Then a function $f()$ is run on the left and right halves, and the key
 - The key is shifted for each round
 - A final permutation (P^{-1})
- Why permuting?
 - mhmm..



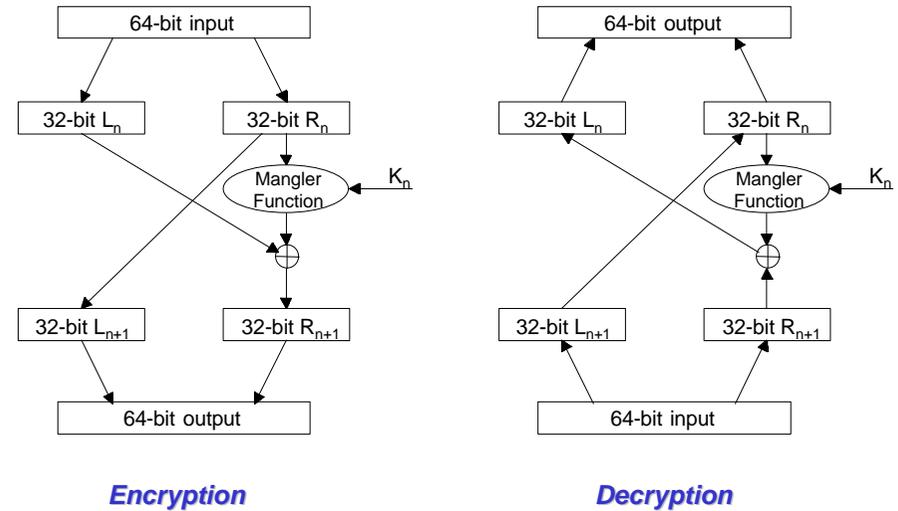
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Initial Permutation IP

- first step of the data computation
- IP reorders the input data bits
- even bits to LH half, odd bits to RH half
- quite regular in structure (easy in HW)
- example:
IP(675a6967 5e5a6b5a) = (ffb2194d 004df6fb)

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DES Round



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DES Round

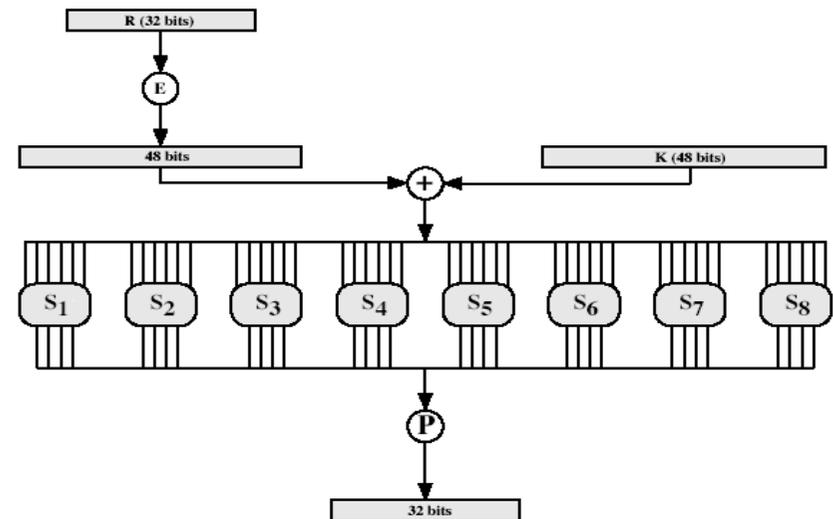
- uses two 32-bit L & R halves
- as for any Feistel cipher can describe as:

$$L_i = R_{i-1}$$

$$R_i = L_{i-1} \oplus f(R_{i-1}, K_i)$$
- Mangler Function details
 - Take 48 bits of the shifted key
 - Expand the right 32-bits of the data to 48 bits
 - XOR the two together, send it through "S-Box"
 - The S-BOX is a predefined substitution table
 - The S-BOX produces 32 new bits, which is XORed with the left half
- Incredibly, this process is reversible

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DES Round: Mangler Function



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DES Round: Mangle Function

- Uses 8 (6x4) S-boxes
 - 6 input bytes yields 4 output bytes
 - each S-box is actually 4 little 4 bit boxes
 - outer bits 1 & 6 select one of the 4 little boxes
 - inner bits 2-5 are substituted
 - result is 8 groups of 4 bits (32 bits)
 - simply a lookup table of 8 x 4 rows and 16 columns
 - 4 rows for each S-box
 - outer bits 1 & 6 (**row** bits) select one of the 4 rows
 - inner bits 2-5 (**col** bits) are substituted
- Example:
 - Given bits 110011 as input and S-box 6 from DES
 - Take first and last bits "11" to choose row 3
 - Take middle four bits "1001" to choose column 9
 - The value from S-box 6 of DES is 14 ("1110")
 - Substitute "110011" to "1110"
 - Always count rows and columns from 0 not 1

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DES Round: S-boxes

S ₁															
14	4	13	1	2	15	11	8	3	10	6	12	5	9	0	7
0	15	7	4	14	2	13	1	10	6	12	11	9	8	3	8
4	1	14	8	13	6	2	11	15	12	9	7	3	10	5	0
15	12	8	2	4	9	1	7	5	11	3	14	10	0	6	13

S ₂															
15	1	8	14	6	11	3	4	9	7	2	13	12	0	5	10
3	13	4	7	15	2	8	14	12	0	1	10	6	9	11	5
0	14	7	11	10	4	13	1	5	8	12	6	9	3	2	15
13	8	10	1	3	15	4	2	11	6	7	12	0	5	14	9

S ₃															
10	0	9	14	6	3	15	5	1	13	12	7	11	4	2	8
13	7	0	9	3	4	6	10	2	8	5	14	12	11	15	1
13	6	4	9	8	15	3	0	11	1	2	12	5	10	14	7
1	10	13	0	6	9	8	7	4	15	14	3	11	5	2	12

S ₄															
7	13	14	3	0	6	9	10	1	2	8	5	11	12	4	15
13	8	11	5	6	15	0	3	4	7	2	12	1	10	14	9
10	6	9	0	12	11	7	13	15	1	3	14	5	2	8	4
3	15	0	6	10	1	13	8	9	4	5	11	12	7	2	14

S ₅															
2	12	4	1	7	10	11	6	8	5	3	15	13	0	14	9
14	11	2	12	4	7	13	1	5	0	15	10	3	9	8	6
4	2	1	11	10	13	7	8	15	9	12	5	6	3	0	14
11	8	12	7	1	14	2	13	6	15	0	9	10	4	5	3

S ₆															
12	1	10	15	9	2	6	8	0	13	3	4	14	7	5	11
10	15	4	2	7	12	9	5	6	1	13	14	0	11	3	8
9	14	15	5	2	8	12	3	7	0	4	10	1	13	11	6
4	3	2	12	9	5	15	10	11	14	1	7	6	0	8	13

S ₇															
4	11	2	14	15	0	8	13	3	12	9	7	5	10	6	1
13	0	11	7	4	9	1	10	14	3	5	12	2	15	8	6
1	4	11	13	12	3	7	14	10	15	6	8	0	5	9	2
6	11	13	8	1	4	10	7	9	5	0	15	14	2	3	12

S ₈															
13	2	8	4	6	15	11	1	10	9	3	14	5	0	12	7
1	15	13	8	10	3	7	4	12	5	6	11	0	14	9	2
7	11	4	1	9	12	14	2	0	6	10	13	15	3	5	8
2	1	14	7	4	10	8	13	15	12	9	0	3	5	6	11

Example:

S(18 09 12 3d 11 17 38 39) = 5fd25e03

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DES Decryption

- decrypt must unwind steps of data computation
- with Feistel design, do encryption steps again
- using subkeys in reverse order (SK16 ... SK1)
- note that IP undoes final FP step of encryption
- 1st round with SK16 undoes 16th encrypt round
-
- 16th round with SK1 undoes 1st encrypt round
- then final FP undoes initial encryption IP
- thus recovering original data value

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Avalanche Effect (Effetto valanga)

- key desirable property of encryption alg
 - where a change of one input or key bit results in changing approx half output bits
 - making attempts to "home-in" by guessing keys impossible
- DES exhibits strong avalanche

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Strength of DES – Key Size

- 56-bit keys have $2^{56} = 7.2 \times 10^{16}$ values
- Originally complaints that the NSA fixed the S-boxes to provide a backdoor. This has never been found
 - **The S-boxes appear to be strong against even differential cryptanalysis (Which means the NSA knew about DC before 1978. It was first described publicly in 1990)**
- Algorithm has never been “broken”
 - **Successfully attacked by brute force**
- Recent advances have shown is possible to break by brute force
 - **in 1997 on Internet in a few months**
 - **in 1998 on dedicated HW (\$250K) in a few days (Electronic Frontier Foundation)**
 - **in 1999 above (EFF) combined in 22hrs!**
 - **reasonable for a small business to buy**
- Still must be able to recognize plaintext

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3-DES, IDEA, AES

Triple DES: Why?

- The keyspace of DES is too small
- Clear a replacement for DES was needed
 - **theoretical attacks that can break it**
 - **demonstrated exhaustive key search attacks**
- AES is a new cipher alternative
- Prior to this alternative was to use multiple encryption with DES implementations
- Triple-DES is the chosen form

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Multiple Encryption DES

- A possible solution is to use the same encryption algorithm more times
- Both Encryption and Decryption algorithms can be see as encryption functions
- How many time should be performed? (2,3,4, 1000..)
- How many keys?
- What combination of E and D can be chosen? (EEE, ED, etc)

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How many time should be performed?

- The more time the block is encrypted the more secure it is
- For computation, no more encryptions than are necessary
- Encrypting twice with the same key
 - plaintext \xrightarrow{K} \xrightarrow{K} ciphertext
 - no more secure than single encryption with K: exhaustive search requires trying 2^{56} keys
- Encrypting twice with two keys
 - plaintext $\xrightarrow{K_1}$ $\xrightarrow{K_2}$ ciphertext
 - there is an attack (not very practical) that breaks doubling DES in roughly twice the time of a brute-force breaking single DES
 - since $X = E_{K_1}[P] = D_{K_2}[C]$
 - attack by encrypting P with all keys and store
 - then decrypt C with keys and match X value
 - can show takes $O(2^{56})$ steps
- Triple encryption with two keys (EDE)

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Triple DES (3-DES)



- lunghezza blocco = 64 bit
- chiave (k, k', k'') lunga $56 + 56 + 56 = 168$ bit
- lunghezza blocco = 64 bit
- chiave (k, k') lunga $56+56 = 112$ bit
 - K_1 to E, K_2 to D, K_1 to E
- spesso chiamato EDE (acronimo per **Encrypt Decrypt Encrypt**) or TDEA
- adottato negli standard X9.17 e ISO 8732

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Triple-DES with Two-Keys

- Use 2 keys K_1 and K_2 with E-D-E sequence
 - $C = E_{K_1}[D_{K_2}[E_{K_1}[P]]]$
- A key space of 2^{112} possible keys
- Encrypt & decrypt are equivalent in security: there is no advantage to using decryption for the second stage
- however, if $K_1 = K_2$ we have backwards compatibility
 - $E_{K_1}(D_{K_1}(E_{K_1}(P))) = E_{K_1}(P)$
- Standardized in ANSI X9.17 & ISO8732
- No current known practical attacks

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Triple-DES with Three-Keys

- Triple-DES with Three-Keys
 - $C = E_{K_3}[D_{K_2}[E_{K_1}[P]]]$
- Although there are no practical attacks on two-key
- Has been adopted by some Internet applications, eg PGP, S/MIME

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Altri cifrari

- IDEA (International Data Encryption Algorithm) [1990]
- SAFER (Secure And Fast Encryption Routine)
SAFER K-64 [1994], SAFER K-128 [1995]
- RC5 [1995]

cifrario	bit chiave	bit testo
IDEA	128	64
SAFERK-64	64	64
SAFERK-128	128	64
RC5	<256 byte	32,64,128

- Madryga, NewDES, FEAL, REDOC, LOKI, Khufu, Knafre, RC2, MMB, GOST, Blowfish, ...
- ... AES

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IDEA

- International Data Encryption Algorithm
 - **Used in PGP (Pretty Good Privacy)**
- Similar to DES
 - **Works on 64-bit input blocks**
 - Taken as 4 16-bit blocks
 - **Uses a 128-bit key**
 - Uses a total of 52 16-bit subkeys
(17 rounds : 4 keys+2 keys+4 keys+ .. +4keys=52)
 - **operates in rounds (17 rounds)**
 - **complicated mangler function that does not have to be reversible (it is run in the same direction for both encryption/decryption as for DES)**
 - **Decryption uses same algorithm**
 - Different subkey generation
- Encryption/decryption keys (not as DES) are related in complex manner

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Blowfish

- A symmetric block cipher designed by Bruce Schneier in 1993/94
- Characteristics
 - **fast implementation on 32-bit CPUs**
 - **compact in use of memory**
 - **simple structure eases analysis/implementation**
 - **variable security by varying key size (uses a 32 to 448 bit key)**
- Has been implemented in various products

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AES

- Designed to replace DES
 - **Organized by NIST**
 - **Chosen from five candidate algorithms**
 - Reviewed by US government (NSA), industry and academia
 - Required a four-year process to pick the algorithm
 - Winning algorithm chosen 2 Oct 2000
 - Rijndael Block Cipher
 - Joan Daemon, Vincent Rijmen (Belgium)
 - Has become a NIST standard

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AES

- Key sizes
 - The AES will specify three key sizes: 128, 192 and 256 bits. In decimal terms, this means that there are approximately:
 - 3.4×10^{38} possible 128-bit keys;
 - 6.2×10^{57} possible 192-bit keys; and
 - 1.1×10^{77} possible 256-bit keys.
 - In comparison, DES keys are 56 bits long, which means there are approximately 7.2×10^{16} possible DES keys. Thus, there are on the order of 10^{21} times more AES 128-bit keys than DES 56-bit keys

- Will the AES replace Triple DES and DES?
 - The AES is being developed to replace DES, but NIST anticipates that Triple DES will remain an approved algorithm (for U.S. Government use)

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AES robustness

- Brute force attack
 - In the late 1990s, specialized "DES Cracker" machines were built that could recover a DES key after a few hours. In other words, by trying possible key values, the hardware could determine which key was used to encrypt a message
 - If you could crack a DES key in one second (i.e., try 2^{56} keys per second), it would take 149 trillion years to crack a 128-bit AES key by brute force at the same speed
 - the universe is believed to be less than 20 billion years old
 - But, things change...

- AES robustness
 - No one can be sure how long the AES - or any other cryptographic algorithm - will remain secure
 - However, DES was a U.S. Government standard for approximately twenty years before it was known to be "cracked" by massive parallel computer
 - AES has the potential to remain secure well beyond twenty years

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Comparison of symmetric key algorithms

Speed Comparisons of Block Ciphers on a Pentium

Algorithm	Clock cycles per round	# of rounds	# of clock cycles per byte encrypted
Blowfish	9	16	18
RC5	12	16	23
DES	18	16	45
IDEA	50	8	50
Triple-DES	18	48	108

Encrypting Large Messages

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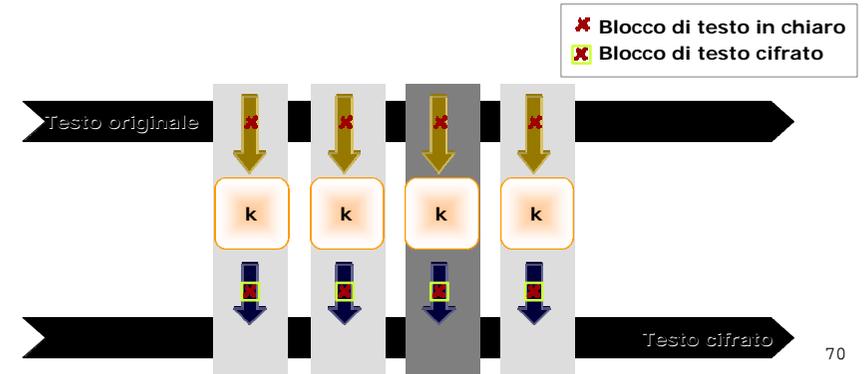
Encrypting large messages

- Block ciphers encrypt fixed size blocks
 - eg. **DES encrypts 64-bit blocks, with 56-bit key**
- Need way to use in practise, given usually have arbitrary amount of information to encrypt (longer than 64bits..)
- Four were defined for DES in ANSI standard ANSI X3.106-1983 Modes of Use
- These schemes are applicable for DES, 3DES, IDEA, EAS, etc
- Modes:
 - Electronic Code Book (ECB)
 - Cipher Block Chaining (CBC)
 - k-bit Cipher Feedback Mode (CFB)
 - k-bit Output Feedback Mode (OFB)

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Electronic Codebook (ECB)

- Consist of doing the obvious thing, and it is usually the worst method.. ;)
- The message is broke into 64-bit blocks, with padding for the last one
- Each block is independently encrypted with the secret key
 - $C_i = \text{DES}_{K_1}(P_i)$
 - each block is a value which is substituted, like a codebook



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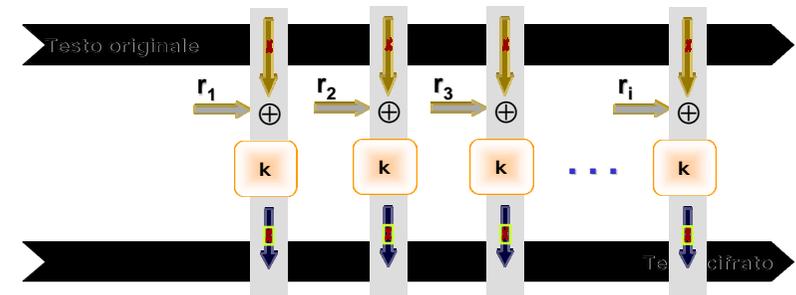
Advantages and Limitations of ECB

- At end of message, handle possible last short block
 - by padding either with known non-data value (eg nulls)
 - or pad last block with count of pad size
 - eg. [b1 b2 b3 0 0 0 5] <- 3 data bytes, then 5 bytes pad+count
- There are a number of problem that arise and that don't show up in the single block case
 - Repetitions in message may show in ciphertext if aligned with message block
 - if a message contains 2 identical 64-bit blocks, the corresponding cipher blocs are identical; it can be a problem
 - in some cases it can be possible to guess a portion of the message
 - in some cases it can be possible to alter the message
- As result, ECB is rarely used
 - main use is sending a few blocks of data

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Cipher Block Chaining (CBC)

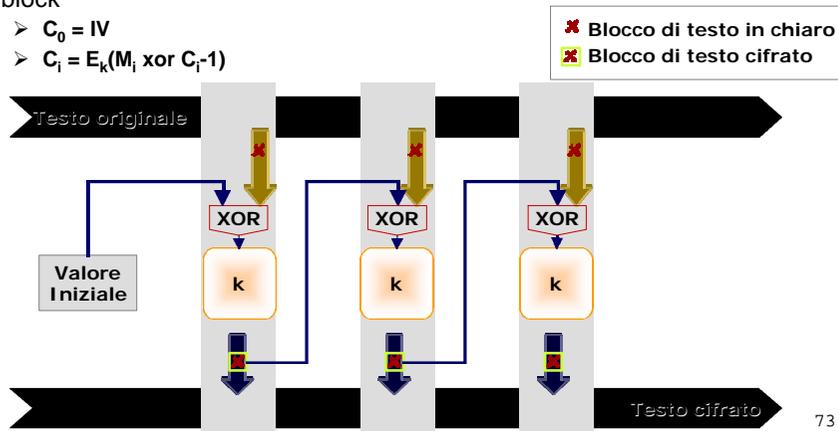
- CBC avoids some problems in ECB
- If the same block repeats in the plain text, it will not cause repeats of ciphertext
- Adds a feedback mechanism to the cipher
- Plaintext is more difficult to manipulate
- Basic idea:



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Cipher Block Chaining (CBC)

- Plaintext patterns are concealed by XORing this block of M with the previous block of C
- Requires an IV (Initialization vector) of random data to encrypt the first block
 - $C_0 = IV$
 - $C_i = E_k(M_i \text{ xor } C_{i-1})$



Advantages and Limitations of CBC

- Decryption is simple because \oplus is reversible
- CBC has the same performance of ECB, except for the cost of generating and transmitting the IV
- Each ciphertext block depends on **all** message blocks
 - thus a change in the message affects all ciphertext blocks after the change as well as the original block
- It can be used the value of 0 as IV, however it can lead to some problems
 - e.g. if a message is transmitted weekly, it is possible to guess if changes occurred
 - Moreover, $IV \neq 0$ prevents attackers for supplying chosen plaintext
- If IV is sent in the clear, an attacker can change bits of the first block, and change IV to compensate
 - hence either IV must be a fixed value (as in EFTPOS) or it must be sent encrypted in ECB mode before rest of message

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CBC Threat 1 - Modifying ciphertext blocks

- Using CBC does not eliminate the problem of someone modifying the message in transit
- If the attacker changes the ciphertext block c_n , c_n gets \oplus 'd with the decrypted c_{n+1} to yield m_{n+1}
 - changing bit h of c_n has predictable effect to bit h of m_{n+1}
 - the attacker cannot know the new m_n (a new random 64-bit value, as side effect)
- This threat can be combated by adding a CRC to the plaintext before encrypt

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CBC Threat 2 - Rearranging ciphertext blocks

- Knowing the plain text, the corresponding ciphertext and IV, it is possible to rearrange the c_1, c_2, c_3, \dots (building blocks), in such a way to obtain a new m_1, m_2, m_3, \dots
- A CRC can help but not solve the problem (1 in 2^{32} chance that the CRC will work; if the attack consist only in modifying the message, it is possible to try several combination)

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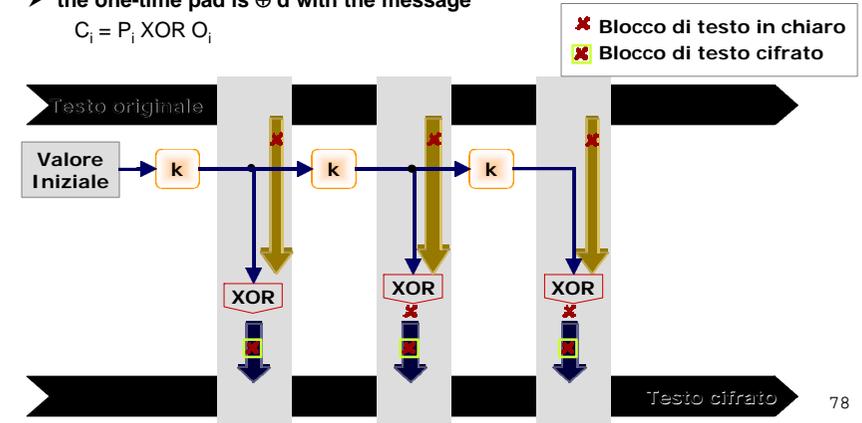
Output Feedback (OFB)

- Acts like a pseudorandom number generator
- The message is encrypted by \oplus ing it with the pseudorandom stream generated by the OFB
 - message is treated as a stream of bits
- How it works:
 - A pseudorandom number O_0 is generated (named IV as in CBC)
 - O_0 is encrypted (using secret key K) obtaining O_1
 - from O_1 is obtained O_2 and so on, as many block are needed
 - $O_i = E_K(O_{i-1})$
 - $O_0 = IV$
 - feedback is independent of message and can be computed in advance
 - so, a long pseudorandom string is generated (one-time pad)
 - the one-time pad is simply \oplus 'd with the message
 - $C_i = P_i \text{ XOR } O_i$
- Uses: stream encryption over noisy channels

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Output Feedback (OFB)

- OFB in short:
 - a long pseudorandom string is generated (one-time pad)
 - $O_i = E_K(O_{i-1})$
 - $O_0 = IV$
 - the one-time pad is \oplus 'd with the message
 - $C_i = P_i \text{ XOR } O_i$



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Advantages and Limitations of OFB

- Advantages of OFB:
 - one-time pad can be generated in advances
 - if some bits of the ciphertext get garbled, only those bits of plaintext get garbled (no error propagation)
 - if a message arrives in arbitrary-sized chunks, the associated ciphertext can immediately be transmitted
- Disadvantages of OFB:
 - sender and receiver must remain in sync, and some recovery method is needed to ensure this occurs
 - if the plaintext and the ciphertext is known by a bad guy, he can modify the plaintext into anything he wants
 - hence must never reuse the same sequence (key+IV)

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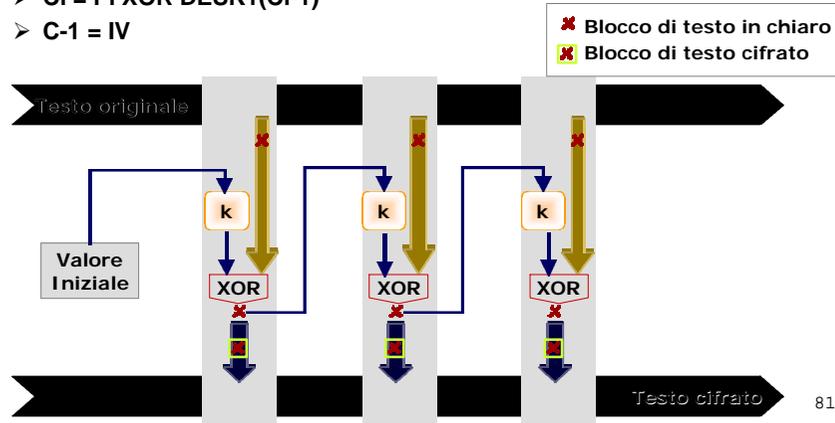
Cipher FeedBack (CFB)

- Very similar to OFB
- The k -bit shifted in to the encryption module are the k -bit of the ciphertext from the previous block
- added to the output of the block cipher
- result is feed back for next stage (hence name)
 - $C_i = P_i \text{ XOR } \text{DES}_{k1}(C_{i-1})$
 - $C_{-1} = IV$

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Cipher Feedback (CFB)

- Very similar to OFB
- The k-bit shifted in to the encryption module are the k-bit of the ciphertext from the previous block
 - $C_i = P_i \text{ XOR } \text{DESK}_1(C_{i-1})$
 - $C_{-1} = \text{IV}$



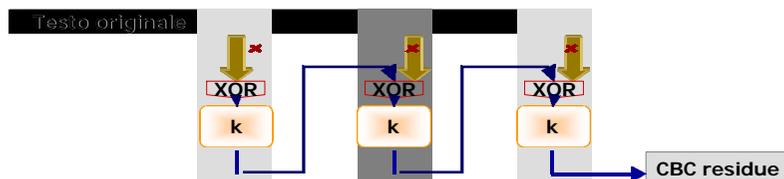
Advantages and Limitations of CFB

- Note: the block cipher is used in **encryption** mode at **both** ends
- The one-time pad cannot be generated in CFB
- Limitation is need to stall while do block encryption after every n-bits
- Errors propagate for several blocks after the error
- it is possible to have k-bit CFB with k different from 64 (e.g. 8)
 - With OFB or CBC if character are lost in transmission or extra character are added, the rest of trasmission is garbled
 - With 8-bit CFB as long as an error is an integral number of bytes, things will be resynchronized
 - a disadvantage is that DES operation is required each byte

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Integrity: Generating MICs

- CBC, CFB and OFB, when properly used, offer good protection against an eavesdropper deciphering a message
- None of these offers good protection against an eavesdropper (who already knows the plaintext or not) modifying it undetected
 - note that any random string of bits will decrypt into something)
- In many context message are not secret but integrity must be assured
- A secret key system can be used to generate a cryptographic checksum known as MIC (Message Integrity Code)
- A standard way of protection is to compute the CBC but send only the last block (named CBC residue) along with the plaintext



Ensuring Privacy and Integrity

- To assure privacy it is possible to CBC-encrypt the message
- To assure integrity is appropriate to transmit unencrypted data plus a CBC residue
- To assure both privacy and integrity, is not sufficient to CBC-encrypt the message, nor sending together a CBC-residue
- A possible solution is to send CBC-encrypted message with a CBC-residue, computed with two different keys
 - **double complexity!**

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Ensuring Privacy and Integrity

- Other possible solutions:
 - **CBC with a weak cryptography checksum**
 - e.g. Kerberos V4
 - **CBC with cryptography hash**
 - two cryptographic computations such as CBC with two different keys, but more efficient (thanks to hash algorithms)
 - e.g. with MD4, MD5, etc
 - **CBC encryption and CBC residue with related keys**
 - it could be sufficient to switch just one bit
 - e.g. kerberos V5 \oplus s the key with `0xF0F0F0F0F0F0F0`
 - this has the property of preserving key parity and never transforming non-weak key into a weak-key