



UNIVERSITA' DEGLI STUDI DI PARMA  
Dipartimento di Ingegneria dell'Informazione

## Secret Key (symmetric) Cryptography

Luca Veltri

(mail.to: luca.veltri@unipr.it)

Corso di Sicurezza nelle reti di telecomunicazioni, a.a. 2004/2005  
<http://www.tlc.unipr.it/veltri>



Università degli Studi di Parma  
Dipartimento di Ingegneria dell'Informazione

Symmetric Cryptography

## Symmetric Encryption

- Or conventional / private-key / single-key
- Sender and recipient share a common key
- All classical encryption algorithms are private-key
- Was the only type prior to invention of public-key in 1970's
- Secret key cryptographic systems are designed to take a reasonable-length key (e.g. 64 bits) and generating a one-to-one mapping that "looks like completely **random**", to someone doesn't know the key

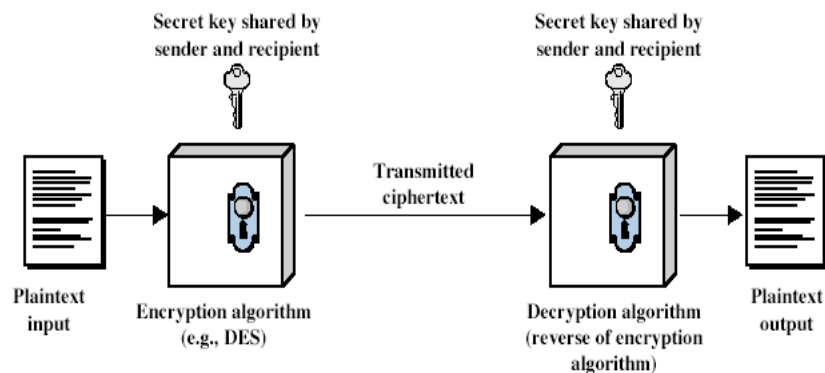
2



Università degli Studi di Parma  
Dipartimento di Ingegneria dell'Informazione

Symmetric Cryptography

## Symmetric Cipher Model



3



Università degli Studi di Parma  
Dipartimento di Ingegneria dell'Informazione

Symmetric Cryptography

## Symmetric Cipher Model

- two requirements for secure use of symmetric encryption:
  - a **strong encryption algorithm**
  - a **shared secret key known only to sender / receiver**
- plaintext =  $m$
- ciphertext =  $c = E_k(m)$
- decrypted plaintext =  $D_k(c) = D_k(E_k(m)) = m$
- assume encryption algorithm is known
- implies a secure channel to distribute key

4

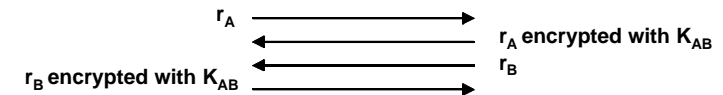
## Symmetric Cipher Characteristics

- Richiede una fase iniziale in cui ciascuna coppia di interlocutori si scambia la secret key in maniera sicura
- Il numero delle chiavi per realizzare una comunicazione reciproca tra  $N$  utenti (dispositivi) è pari a  $N \times (N-1)/2$  (se le chiavi rimangono sempre le stesse)
- Viene generalmente utilizzato per proteggere, mediante codifica, informazioni (file) in un repository locale o trasmessi
- La robustezza dell'algoritmo è normalmente misurata dalla lunghezza delle chiavi: 40 bit (debole), 128 bit (forte)
- Algoritmi più diffusi: DES, 3DES, RC2, RC4, IDEA, AES

5

## Security uses of secret key cryptography

- Transmitting over an insecure channel
  - **the two parties agree on a shared secret key and use secret key cryptography to send messages**
- Secure storage on insecure media
  - **the user uses a secret key to store and retrieve data on an (insecure) media**
- Authentication
  - **strong authentication through a challenge-response mechanism**



- Integrity check
  - **generating a fixed-length cryptographic checksum associated with a message (Message Integrity Code - MIC)**

6

## Difetti dei sistemi simmetrici

- Metodo per scambio di chiavi assente
- Numero di chiavi troppo grande per gestire dei segreti condivisi tra singoli utenti  
[  $n(n-1)/2$  ]

7

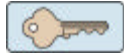
## Classical Substitution Ciphers

- where letters of plaintext are replaced by other letters or by numbers or symbols
- or if plaintext is viewed as a sequence of bits, then substitution involves replacing plaintext bit patterns with ciphertext bit patterns

8

## Crittografia classica con sostituzione: esempi

### Cifrario con shift



Chiave  $K \in \{0, 1, \dots, 25\}$

$$X_i \leftarrow M_i + K \bmod 26$$

### Cifrario monoalfabetico



Chiave

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| O | C | T | M | B | W | L | A | K | J | D | X | I | N | E | Y | S | U | P | F | Z | R | Q | H | V | G |

testo in chiaro: C A S A

testo cifrato: T O P O

9

## Caesar Cipher

- earliest known substitution cipher
- by Julius Caesar
- first attested use in military affairs
- replaces each letter by 3rd letter on
- example:  
meet me after the toga party  
PHHW PH DIWHU WKH WRJD SDUWB

10

## Caesar Cipher (cont.)

- can define transformation as:  
a b c d e f g h i j k l m n o p q r s t u v w x y z  
D E F G H I J K L M N O P Q R S T U V W X Y Z A B C
- mathematically give each letter a number  
a b c d e f g h i j k l m  
0 1 2 3 4 5 6 7 8 9 10 11 12  
n o p q r s t u v w x y z  
13 14 15 16 17 18 19 20 21 22 23 24 25
- then have Caesar cipher as:  
 $C = E(p) = (p + k) \bmod (26)$   
 $p = D(C) = (C - k) \bmod (26)$

11

## Monoalphabetic Cipher

- rather than just shifting the alphabet
- could shuffle (jumble) the letters arbitrarily
- each plaintext letter maps to a different random ciphertext letter
- hence key is 26 letters long

Plain: abcdefghijklmnopqrstuvwxyz  
Cipher: DKVQFIBJWPESCXHTMYAUOLRGZN

Plaintext: ifwewishtoreplaceletters  
Ciphertext: WIRFRWAJUHYFTSDVFSFUUFYA

12

## Monoalphabetic Cipher Security

- now have a total of  $26! = 4 \times 10^{26}$  keys
- with so many keys, might think is secure
- but would be WRONG!!
- problem is language characteristics
  - letter frequencies
  - most common words
  - two letters frequencies (e.g. "th" in english)
  - etc.

13

## Polyalphabetic Ciphers

- another approach to improving security is to use multiple cipher alphabets
- called **polyalphabetic substitution ciphers**
- makes cryptanalysis harder with more alphabets to guess and flatter frequency distribution
- use a key to select which alphabet is used for each letter of the message
- use each alphabet in turn
- repeat from start after end of key is reached

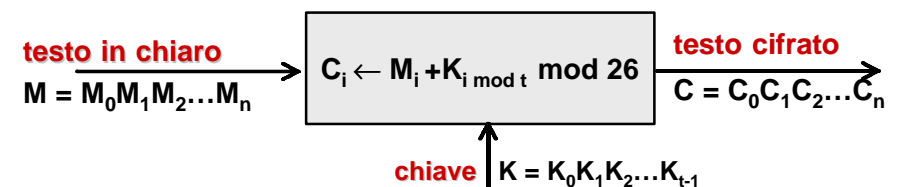
14

## Vigenère Cipher

- simplest polyalphabetic substitution cipher is the **Vigenère Cipher** [1586]
  - (Blaise de Vigenère, 1523-1596)
- effectively multiple caesar ciphers
- key is multiple letters long  $K = k_1 k_2 \dots k_d$
- $i^{\text{th}}$  letter specifies  $i^{\text{th}}$  alphabet to use
- use each alphabet in turn
- repeat from start after  $d$  letters in message
- decryption simply works in reverse

15

## Vigenère Cipher (cont.)



### Esempio

Testo in chiaro: CODICE MOLTO SICURO

Chiave: REBUS

|         |       |       |       |    |          |
|---------|-------|-------|-------|----|----------|
|         | CODIC | EMOLT | OSICU | RO | testo in |
| chiaro  |       |       |       |    |          |
|         | REBUS | REBUS | REBUS | RE | chiave   |
|         | TSECU | VQPFL | FWJWM | IS | testo    |
| cifrato |       |       |       |    |          |

16

## Cryptanalysis of Vigenère Ciphers

- have multiple ciphertext letters for each plaintext letter
- hence letter frequencies are obscured
- but not totally lost
- start with letter frequencies
  - **see if look monoalphabetic or not**
- if not, then need to determine number of alphabets, since then can attach each

17

## One-Time Pad

- if a truly random key as long as the message is used, the cipher will be secure
- called a One-Time pad
- Advantages:
  - **is unbreakable since ciphertext bears no statistical relationship to the plaintext, and**
  - **for any plaintext & any ciphertext there exists a key mapping one to other**
- Disadvantages:
  - **can only use the key once**
  - **have problem of safe distribution of key**

18

## Transposition Ciphers

- another technique is that used by classical **transposition** or **permutation** ciphers
- these hide the message by rearranging the letter order (blocks of bits)
- without altering the actual letters used
- can recognise these since have the same frequency distribution as the original text

19

## Example: Row Transposition Ciphers

- a more complex scheme
  - write letters of message out in rows over a specified number of columns
  - then reorder the columns according to some key before reading off the rows
- ```
Key:      4 3 1 2 5 6 7
Plaintext: a t t a c k p
           o s t p o n e
           d u n t i l t
           w o a m x y z
Ciphertext: TTNAAPTMTSUOAODWCOIXKNLYPETZ
```

20

## Product Ciphers

- Ciphers using substitutions or transpositions are not secure because of language characteristics
- Hence consider using several ciphers in succession to make harder:
  - **two substitutions make a more complex substitution**
  - **two transpositions make more complex transposition**
  - **but a substitution followed by a transposition makes a new much harder cipher**
- This is bridge from classical to modern ciphers

21

## Rotor Machines

- Before modern ciphers, rotor machines were most common product cipher
- Were widely used in WW2
  - **German Enigma, Allied Hagelin, Japanese Purple**
- Implemented a very complex, varying substitution cipher
- Used a series of cylinders, each giving one substitution, which rotated and changed after each letter was encrypted
- with 3 cylinders have  $26 \times 26 \times 26 = 26^3 = 17576$  alphabets

22

## Steganography

- an alternative to encryption
- hides existence of message
  - **using only a subset of letters/words in a longer message marked in some way**
  - **using invisible ink**
  - **hiding in graphic image or sound file**
- has drawbacks
  - **high overhead to hide relatively few info bits**

## Block and Stream Ciphers

23

## Block and Stream Ciphers

- There are two basic cipher structures
  - **Block ciphers**
    - Block ciphers process messages in into blocks, each of which is then en/decrypted
    - Plaintext is treated as a sequence of n-bit blocks of data
    - Ciphertext is same length as plaintext
    - Like a substitution on very big characters (64-bits or more)
    - Can be made to behave as a stream cipher
  - **Stream ciphers**
    - Stream ciphers process messages (Encryption/Decryption) a bit or byte at a time when en/decrypting
    - Often easier to analyze mathematically
- many current ciphers are block ciphers

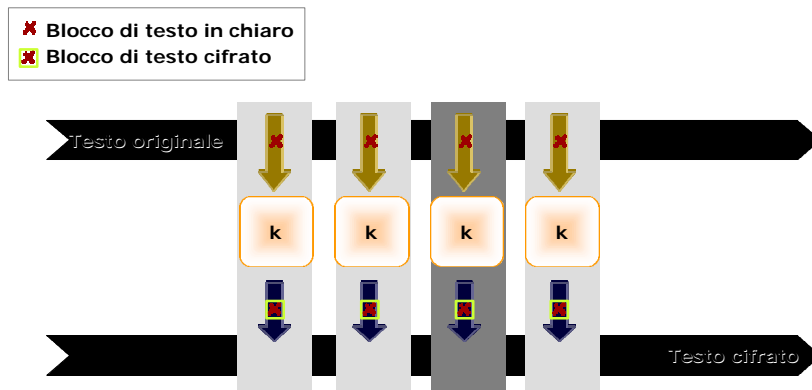
25

## Block Ciphers

- A cryptographic algorithm convert a plaintext block into an encrypted block
- How long should the plaintext block be?
  - **having block length too short (say one byte as in monoalphabetic cipher), it could be easier to construct a decryption table starting from some <plaintext,ciphertext> pairs**
  - **having block length too long, it could be inconvenient due to the increasing of complexity**
- 64bit blocks are often used
  - **it is difficult to obtain all  $2^{64}$  pairs(known plaintext attack)..**

26

## Example of Block Ciphers



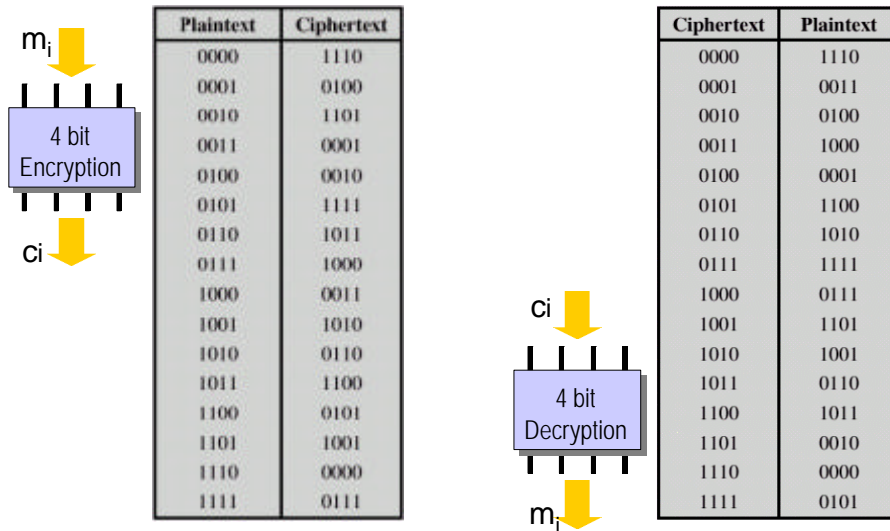
27

## Block Ciphers

- block ciphers look like an extremely large substitution
- If 64bit blocks are used,  $2^{64}$  possible input values are mapped to  $2^{64}$  output values
- The most general way of encrypting could be to specify completely the mapping table
  - **would need table of  $2^{64}$  entries for a 64-bit block  $\rightarrow 2^{70}$  bits!**
  - **it is too long for a key.. ;-)**
  - **instead create from smaller building blocks**

28

## Esempio di crittografia a blocchi di 4 bit



29

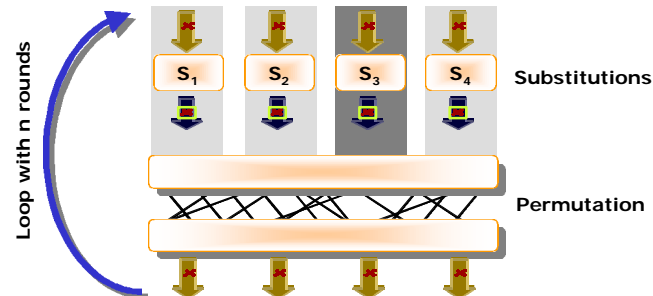
## Block Ciphers

- Two kind of simple transformations are used:
  - **substitutions**
    - specifies for each of the  $2^k$  possible input values the  $k$ -bit output
    - this is not practical for 64-bit blocks, but is possible for lower length blocks (e.g. 8bits)
    - to specify a substitution on  $k$ -bit blocks,  $k \cdot 2^k$  bits are required
  - **permutations**
    - specifies for each of the  $k$  input bits the corresponding output position
    - a permutation is a special case of substitution in which each bit of the output gets its value from exactly one bit of the input
    - to specify a permutation on  $k$ -bit blocks,  $k \cdot \log_2 k$  bits are required

30

## Block Ciphers

- One possible way to build a secret key algorithm is
  - to break the input into managed-sized chunks (say 8 bits),
  - do a substitution on each small chunk,
  - and then take the output of all the substitutions and run them through a permuter (big as the input)
  - the process is repeated, so that each bit winds up as input to each substitution
  - Each time is called *round*



31

## Substitution-Permutation Ciphers

- Cipher needs to completely obscure statistical properties of original message
  - a one-time pad does this
- in 1949 Claude Shannon introduced idea of substitution-permutation (S-P) networks
- S-P networks are based on the two primitive cryptographic operations:
  - **substitution**
  - **permutation**
- these form the basis of modern block ciphers
- provide confusion and diffusion of message
  - **confusion**
    - makes relationship between ciphertext and key as complex as possible
  - **diffusion**
    - dissipates statistical structure of plaintext over bulk of ciphertext
    - every single plaintext cipher will influence several ciphertext ciphers
- the operation must be reversible!

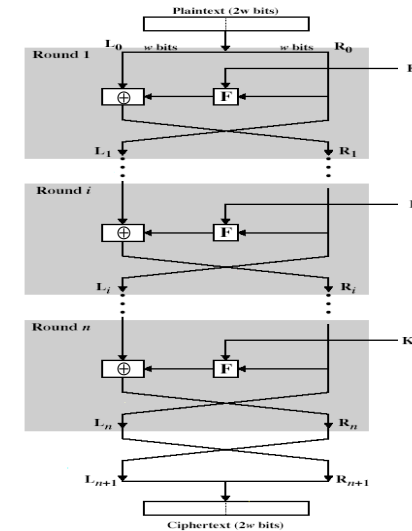
32



## Feistel Cipher Structure

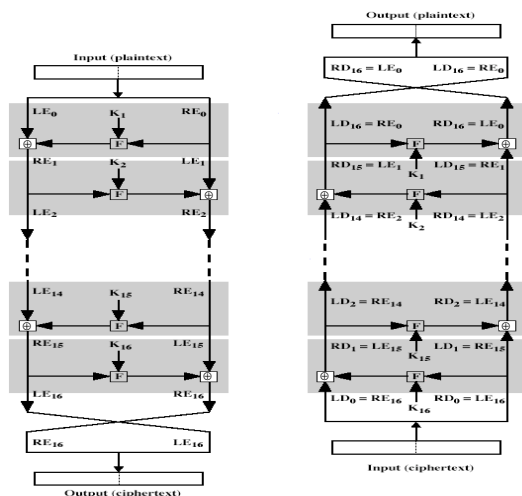
- Horst Feistel devised the **cipher**  
based on concept of invertible product cipher
  - - process through multiple rounds which perform a substitution on left data half
    - then have permutation swapping halves
- implements Shannon's substitution-permutation network concept

## Feistel Cipher Structure



34

## Feistel Cipher Decryption



35

## Design Principles

Block Ciphers are defined in terms of

- **block size**
  - increasing size improves security, but slows cipher
- **key size**
  - increasing size improves security, makes exhaustive key searching harder, but may slow cipher
- **number of rounds**
  - increasing number improves security, but slows cipher
- **subkey generation**
  - greater complexity can make analysis harder, but slows cipher
- **round function**
  - greater complexity can make analysis harder, but slows cipher

Two other considerations

- **fast software en/decryption & ease of analysis**
  - are more recent concerns for practical use and testing

## Data Encryption Standard (DES)

- Most widely used block cipher in world
- Published in 1977 by National Bureau of Standards (now NIST) for use in commercial and unclassified U.S. Government applications
- FIPS PUB 46-3 (Federal Information Processing Standards Publication)
  - U.S. Dept. OF Commerce/NIST (National Institute of Standards and Technology)
- Has widespread use
- Has been considerable controversy over its security

38

## DES History

- Based on an algorithm known as *Lucifer cipher* (1971)
  - by an IBM team led by Horst Feistel
  - used 64-bit data blocks with 128-bit key
- then redeveloped as a commercial cipher with input from NSA and others
- in 1973 NBS issued request for proposals for a national cipher standard
- IBM submitted their revised Lucifer which was eventually accepted as the DES
- DES has become widely used, esp in financial applications
- in 1999 NIST published a new version called *triple DES* (3DES) or *TDEA*

39

## Data Encryption Standard (DES)

- DES encrypts 64-bit data using 56-bit key
- It consists of
  - initial permutation of the 64 bits
  - 16 identical "rounds" of operation where the data is confused and diffused with the key and the previous round
  - A final permutation
- DES can be efficiently implemented in hardware
- Relatively slow if implemented in software
  - this was not a documented goal
  - ..however people have asserted that it was designed with this in mind

40

## DES Design Controversy

- although DES standard is public
- was considerable controversy over design
  - in choice of 56-bit key (vs Lucifer 128-bit)
  - and because design criteria were classified
- subsequent events and public analysis show design was appropriate

41

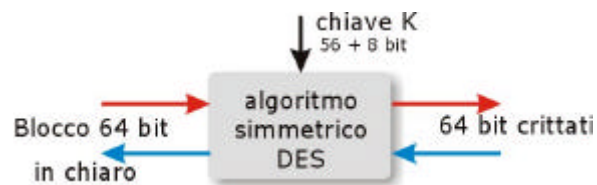
## Why 56bits keys?

- yes.. 8x7 bits + 8 bits for parity check..
- however, 8 bits for parity check are too small
  - 64 bits of garbage have 1 in 256 chance to look like a valid key
- people have suggested that key length has been reduced from 64 to 56 to let DES to be broken (only) by the NSA (15 years ago..)

42

## DES

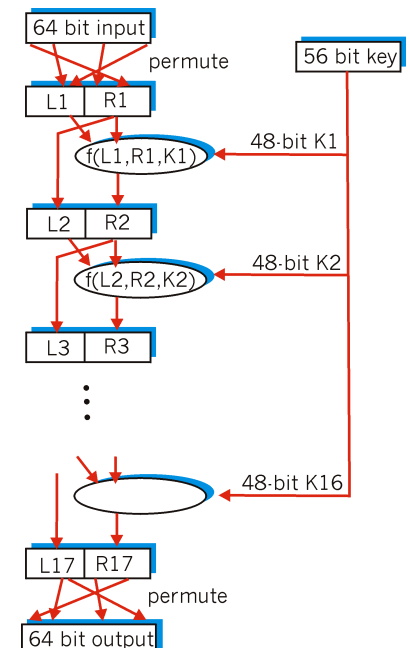
- Uses a 64-bit key that is reduced to 56-bits for parity checking
  - The 56-bit key is transformed in to 16 48-bit subkeys (one per round)
- Transforms 64-bit blocks of input M to 64-bit blocks of output C
- Same algorithm for encryption and decryption (sub-keys are used in reverse order for decryption)



43

## DES

- Consists of
  - An initial permutation (P)
  - Key transformation
    - 16 rounds of:
      - the rightmost 32 bits of the input are moved to the left 32 bits of the output
      - Then a function  $f()$  is run on the left and right halves, and the key
      - The key is shifted for each round
  - A final permutation ( $P^{-1}$ )
- Why permuting?
  - mhmm..

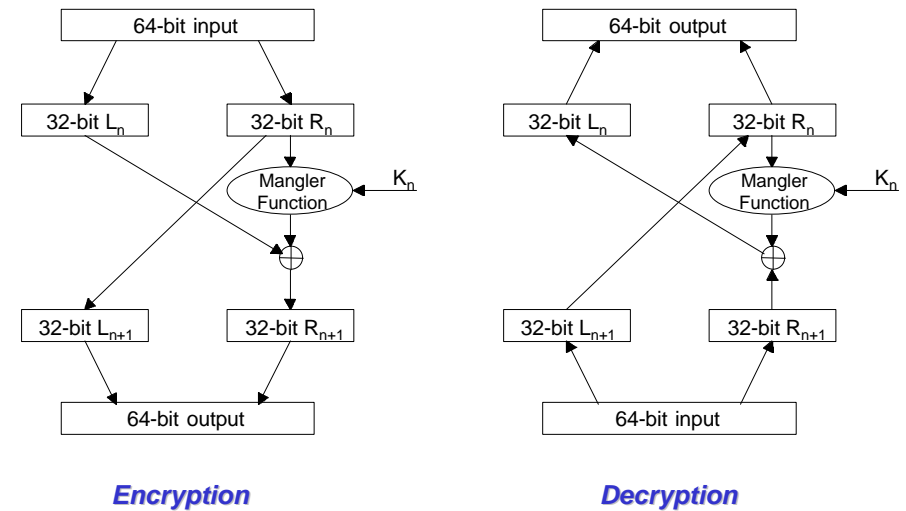


## Initial Permutation IP

- first step of the data computation
- IP reorders the input data bits
- even bits to LH half, odd bits to RH half
- quite regular in structure (easy in HW)
- example:  
 $IP(675a6967\ 5e5a6b5a) = (ffb2194d\ 004df6fb)$

45

## DES Round



46

## DES Round

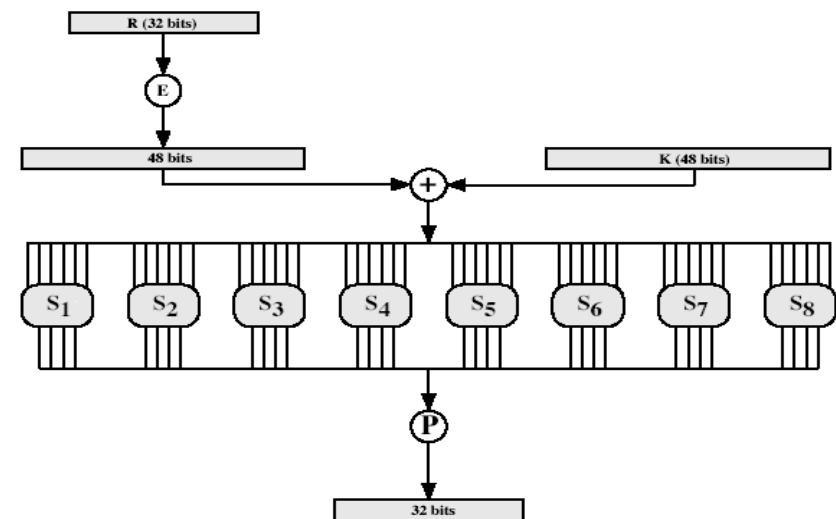
- uses two 32-bit L & R halves
- as for any Feistel cipher can describe as:  

$$L_i = R_{i-1}$$

$$R_i = L_{i-1} \oplus f(R_{i-1}, K_i)$$
- Mangle Function details
  - Take 48 bits of the shifted key
  - Expand the right 32-bits of the data to 48 bits
  - XOR the two together, send it through "S-Box"
  - The S-BOX is a predefined substitution table
  - The S-BOX produces 32 new bits, which is XORed with the left half
- Incredibly, this process is reversible

47

## DES Round: Mangle Function



48

## DES Round: Mangle Function

- Uses 8 (6x4) S-boxes
  - 6 input bytes yields 4 output bytes
  - each S-box is actually 4 little 4 bit boxes
    - outer bits 1 & 6 select one of the 4 little boxes
    - inner bits 2-5 are substituted
    - result is 8 groups of 4 bits (32 bits)
  - simply a lookup table of 8 x 4 rows and 16 columns
    - 4 rows for each S-box
    - outer bits 1 & 6 (row bits) select one of the 4 rows
    - inner bits 2-5 (col bits) are substituted
- Example:
  - Given bits 110011 as input and S-box 6 from DES
    - Take first and last bits "11" to choose row 3
    - Take middle four bits "1001" to choose column 9
    - The value from S-box 6 of DES is 14 ("1110")
    - Substitute "110011" to "1110"
  - Always count rows and columns from 0 not 1

49

## DES Round: S-boxes

|       |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|-------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| $S_1$ |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
| 14    | 4  | 13 | 1  | 2  | 15 | 11 | 8  | 3  | 10 | 6  | 12 | 5  | 9  | 0  | 7  |
| 0     | 15 | 7  | 4  | 14 | 2  | 13 | 1  | 10 | 6  | 12 | 11 | 9  | 5  | 3  | 8  |
| 4     | 1  | 14 | 8  | 13 | 6  | 2  | 11 | 15 | 12 | 9  | 7  | 3  | 10 | 5  | 0  |
| 15    | 12 | 8  | 2  | 4  | 9  | 1  | 7  | 5  | 11 | 3  | 14 | 10 | 0  | 6  | 13 |
| $S_2$ |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
| 15    | 1  | 8  | 14 | 6  | 11 | 3  | 4  | 9  | 7  | 2  | 13 | 12 | 0  | 5  | 10 |
| 3     | 13 | 4  | 7  | 15 | 2  | 8  | 14 | 12 | 0  | 1  | 10 | 6  | 9  | 11 | 5  |
| 0     | 14 | 7  | 11 | 10 | 4  | 13 | 1  | 5  | 8  | 12 | 6  | 9  | 3  | 2  | 15 |
| 13    | 8  | 10 | 1  | 3  | 15 | 4  | 2  | 11 | 6  | 7  | 12 | 0  | 5  | 14 | 9  |
| $S_3$ |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
| 10    | 0  | 9  | 14 | 6  | 3  | 15 | 5  | 1  | 13 | 12 | 7  | 11 | 4  | 2  | 8  |
| 13    | 7  | 0  | 9  | 3  | 4  | 6  | 10 | 2  | 8  | 5  | 14 | 12 | 11 | 15 | 1  |
| 13    | 6  | 4  | 9  | 8  | 15 | 3  | 0  | 11 | 1  | 2  | 12 | 5  | 10 | 14 | 7  |
| 1     | 10 | 13 | 0  | 6  | 9  | 8  | 7  | 4  | 15 | 14 | 3  | 11 | 5  | 2  | 12 |
| $S_4$ |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
| 7     | 13 | 14 | 3  | 0  | 6  | 9  | 10 | 1  | 2  | 8  | 5  | 11 | 12 | 4  | 15 |
| 13    | 8  | 11 | 5  | 6  | 15 | 0  | 3  | 4  | 7  | 2  | 12 | 1  | 10 | 14 | 9  |
| 10    | 6  | 9  | 0  | 12 | 11 | 7  | 13 | 15 | 1  | 3  | 14 | 5  | 2  | 8  | 4  |
| 3     | 15 | 0  | 6  | 10 | 1  | 13 | 8  | 9  | 4  | 5  | 11 | 12 | 7  | 2  | 14 |
| $S_5$ |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
| 2     | 12 | 4  | 1  | 7  | 10 | 11 | 6  | 8  | 5  | 3  | 15 | 13 | 0  | 14 | 9  |
| 14    | 11 | 2  | 12 | 4  | 7  | 13 | 1  | 5  | 0  | 15 | 10 | 3  | 9  | 8  | 6  |
| 4     | 2  | 1  | 11 | 10 | 13 | 7  | 8  | 15 | 9  | 12 | 5  | 6  | 3  | 0  | 14 |
| 11    | 8  | 12 | 7  | 1  | 14 | 2  | 13 | 6  | 15 | 0  | 9  | 10 | 4  | 5  | 3  |
| $S_6$ |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
| 12    | 1  | 10 | 15 | 9  | 2  | 6  | 8  | 0  | 13 | 3  | 4  | 14 | 7  | 5  | 11 |
| 10    | 15 | 4  | 2  | 7  | 12 | 9  | 5  | 6  | 1  | 13 | 14 | 0  | 11 | 3  | 8  |
| 9     | 14 | 15 | 8  | 2  | 8  | 12 | 3  | 7  | 0  | 4  | 10 | 1  | 13 | 11 | 6  |
| 4     | 3  | 2  | 12 | 9  | 5  | 15 | 10 | 11 | 14 | 1  | 7  | 6  | 0  | 8  | 13 |
| $S_7$ |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
| 4     | 11 | 2  | 14 | 15 | 0  | 8  | 13 | 3  | 12 | 9  | 7  | 5  | 10 | 6  | 1  |
| 13    | 0  | 11 | 7  | 4  | 9  | 1  | 10 | 14 | 3  | 5  | 12 | 2  | 15 | 8  | 6  |
| 1     | 4  | 11 | 13 | 12 | 3  | 7  | 14 | 10 | 15 | 6  | 8  | 0  | 5  | 9  | 2  |
| 6     | 11 | 13 | 8  | 1  | 4  | 10 | 7  | 9  | 5  | 0  | 15 | 14 | 2  | 3  | 12 |
| $S_8$ |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
| 13    | 2  | 8  | 4  | 6  | 15 | 11 | 1  | 10 | 9  | 3  | 14 | 5  | 0  | 12 | 7  |
| 1     | 15 | 13 | 8  | 10 | 3  | 7  | 4  | 12 | 5  | 6  | 11 | 0  | 14 | 9  | 2  |
| 7     | 11 | 4  | 1  | 9  | 12 | 14 | 2  | 0  | 6  | 10 | 13 | 15 | 3  | 5  | 8  |
| 2     | 1  | 14 | 7  | 4  | 10 | 8  | 13 | 15 | 12 | 9  | 0  | 3  | 5  | 6  | 11 |

Example:

S(18 09 12 3d 11 17 38 39) = 5fd25e03

50

## DES Decryption

- decrypt must unwind steps of data computation
- with Feistel design, do encryption steps again
- using subkeys in reverse order (SK16 ... SK1)
- note that IP undoes final FP step of encryption
- 1st round with SK16 undoes 16th encrypt round
- ....
- 16th round with SK1 undoes 1st encrypt round
- then final FP undoes initial encryption IP
- thus recovering original data value

51

## Avalanche Effect (Effetto valanga)

- key desirable property of encryption alg
  - where a change of one input or key bit results in changing approx half output bits
  - making attempts to "home-in" by guessing keys impossible
- DES exhibits strong avalanche

52

## Strength of DES – Key Size

- 56-bit keys have  $2^{56} = 7.2 \times 10^{16}$  values
- Originally complaints that the NSA fixed the S-boxes to provide a backdoor. This has never been found
  - **The S-boxes appear to be strong against even differential cryptanalysis (Which means the NSA knew about DC before 1978. It was first described publicly in 1990)**
- Algorithm has never been “broken”
  - **Successfully attacked by brute force**
- Recent advances have shown is possible to break by brute force
  - **in 1997 on Internet in a few months**
  - **in 1998 on dedicated HW (\$250K) in a few days (Electronic Frontier Foundation)**
  - **in 1999 above (EFF) combined in 22hrs!**
  - **reasonable for a small business to buy**
- Still must be able to recognize plaintext

53

## 3-DES, IDEA, AES

## Triple DES: Why?

- The keyspace of DES is too small
- Clear a replacement for DES was needed
  - **theoretical attacks that can break it**
  - **demonstrated exhaustive key search attacks**
- AES is a new cipher alternative
- Prior to this alternative was to use multiple encryption with DES implementations
- Triple-DES is the chosen form

55

## Multiple Encryption DES

- A possible solution is to use the same encryption algorithm more times
- Both Encryption and Decryption algorithms can be seen as encryption functions
- How many times should be performed? (2,3,4, 1000..)
- How many keys?
- What combination of E and D can be chosen? (EEE, ED, etc)

56

## How many time should be performed?

- The more time the block is encrypted the more secure it is
- For computation, no more encryptions than are necessary
- Encrypting twice with the same key
  - **plaintext  $\xrightarrow{K}$  ciphertext**
  - **no more secure that single encryption with K: exhaustive search requires trying  $2^{56}$  keys**
- Encrypting twice with two keys
  - **plaintext  $\xrightarrow{K_1} \xrightarrow{K_2}$  ciphertext**
  - **there is an attack (not very practical) that breaks doubling DES in roughly twice the time of a brute-force breaking single DES**
    - since  $X = E_{K_1}[P] = D_{K_2}[C]$
    - attack by encrypting P with all keys and store
    - then decrypt C with keys and match X value
    - can show takes  $O(2^{56})$  steps
- Triple encryption with two keys (EDE)

57

## Triple DES (3-DES)



- **lunghezza blocco = 64 bit**
- **chiave (k, k', k'') lunga 56 + 56 + 56 = 168 bit**
- **lunghezza blocco = 64 bit**
- **chiave (k, k') lunga 56+56 = 112 bit**
  - $K_1$  to E,  $K_2$  to D,  $K_1$  to E
- **spesso chiamato EDE (acronimo per **Encrypt Decrypt Encrypt**) or TDEA**
- **adottato negli standard X9.17 e ISO 8732**

58

## Triple-DES with Two-Keys

- Use 2 keys  $K_1$  and  $K_2$  with E-D-E sequence
  - **$C = E_{K_1}[D_{K_2}[E_{K_1}[P]]]$**
- A key space of  $2^{112}$  possible keys
- Encrypt & decrypt are equivalent in security: there is no advantage to using decryption for the second stage
- however, if  $K_1 = K_2$  we have backwards compatibility
  - **$E_{K_1}(D_{K_1}(E_{K_1}(P))) = E_{K_1}(P)$**
- Standardized in ANSI X9.17 & ISO8732
- No current known practical attacks

59

## Triple-DES with Three-Keys

- Triple-DES with Three-Keys
  - **$C = E_{K_3}[D_{K_2}[E_{K_1}[P]]]$**
- Although there are no practical attacks on two-key
- Has been adopted by some Internet applications, eg PGP, S/MIME

60

## Altri cifrari

- IDEA (International Data Encryption Algorithm) [1990]
- SAFER (Secure And Fast Encryption Routine)  
SAFER K-64 [1994], SAFER K-128 [1995]
- RC5 [1995]

| cifrario    | bit chiave | bit testo |
|-------------|------------|-----------|
| IDEA        | 128        | 64        |
| SAFER K-64  | 64         | 64        |
| SAFER K-128 | 128        | 64        |
| RC5         | <256 byte  | 32,64,128 |

- Madryga, NewDES, FEAL, REDOC, LOKI, Khufu, Knafre, RC2, MMB, GOST, Blowfish, ...
- ... AES

61

## IDEA

- International Data Encryption Algorithm
  - **Used in PGP (Pretty Good Privacy)**
- Similar to DES
  - **Works on 64-bit input blocks**
    - Taken as 4 16-bit blocks
  - **Uses a 128-bit key**
    - Uses a total of 52 16-bit subkeys  
(17 rounds : 4 keys+2 keys+4 keys+ .. +4keys=52)
  - **operates in rounds (17 rounds)**
  - **complicated mangler function that does not have to be reversible (it is run in the same direction for both encryption/decryption as for DES)**
  - **Decryption uses same algorithm**
    - Different subkey generation
- Encryption/decryption keys (not as DES) are related in complex manner

62

## Blowfish

- A symmetric block cipher designed by Bruce Schneier in 1993/94
- Characteristics
  - **fast implementation on 32-bit CPUs**
  - **compact in use of memory**
  - **simple structure eases analysis/implemention**
  - **variable security by varying key size (uses a 32 to 448 bit key)**
- Has been implemented in various products

63

## AES

- Designed to replace DES
  - **Organized by NIST**
  - **Chosen from five candidate algorithms**
    - Reviewed by US government (NSA), industry and academia
    - Required a four-year process to pick the algorithm
    - Winning algorithm chosen 2 Oct 2000
    - Rijndael Block Cipher
      - Joan Daemon, Vincent Rijmen (Belgium)
    - Has become a NIST standard

64



## AES

- Key sizes
  - The AES will specify three key sizes: 128, 192 and 256 bits. In decimal terms, this means that there are approximately:
    - $3.4 \times 10^{38}$  possible 128-bit keys;
    - $6.2 \times 10^{57}$  possible 192-bit keys; and
    - $1.1 \times 10^{77}$  possible 256-bit keys.
  - In comparison, DES keys are 56 bits long, which means there are approximately  $7.2 \times 10^{16}$  possible DES keys. Thus, there are on the order of  $10^{21}$  times more AES 128-bit keys than DES 56-bit keys
- Will the AES replace Triple DES and DES?
  - The AES is being developed to replace DES, but NIST anticipates that Triple DES will remain an approved algorithm (for U.S. Government use)

65

## AES robustness

- Brute force attack
  - In the late 1990s, specialized "DES Cracker" machines were built that could recover a DES key after a few hours. In other words, by trying possible key values, the hardware could determine which key was used to encrypt a message
  - If you could crack a DES key in one second (i.e., try  $2^{56}$  keys per second), it would take 149 trillion years to crack a 128-bit AES key by brute force at the same speed
  - the universe is believed to be less than 20 billion years old
  - But, things change...
- AES robustness
  - No one can be sure how long the AES - or any other cryptographic algorithm - will remain secure
  - However, DES was a U.S. Government standard for approximately twenty years before it was known to be "cracked" by massive parallel computer
  - AES has the potential to remain secure well beyond twenty years

66

## Comparison of symmetric key algorithms

Speed Comparisons of Block Ciphers on a Pentium

| Algorithm  | Clock cycles per round | # of rounds | # of clock cycles per byte encrypted |
|------------|------------------------|-------------|--------------------------------------|
| Blowfish   | 9                      | 16          | 18                                   |
| RC5        | 12                     | 16          | 23                                   |
| DES        | 18                     | 16          | 45                                   |
| IDEA       | 50                     | 8           | 50                                   |
| Triple-DES | 18                     | 48          | 108                                  |

## Encrypting Large Messages

67

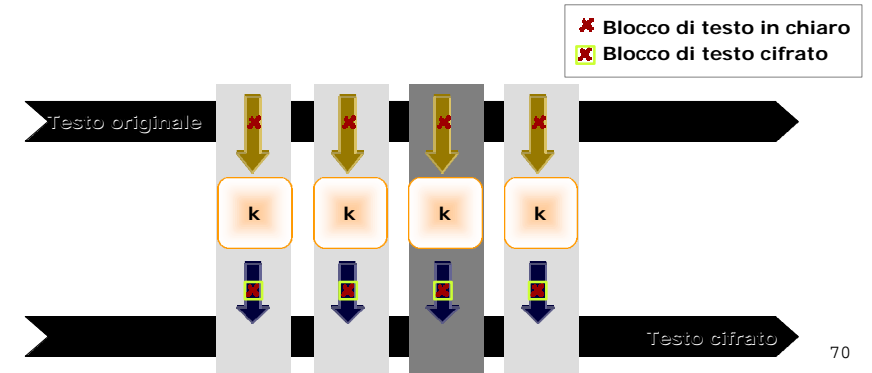
## Encrypting large messages

- Block ciphers encrypt fixed size blocks
  - eg. DES encrypts 64-bit blocks, with 56-bit key
- Need way to use in practise, given usually have arbitrary amount of information to encrypt (longer than 64bits..)
- Four were defined for DES in ANSI standard ANSI X3.106-1983 Modes of Use
- These schemes are applicable for DES, 3DES, IDEA, EAS, etc
- Modes:
  - Electronic Code Book (ECB)
  - Cipher Block Chaining (CBC)
  - k-bit Cipher Feedback Mode (CFB)
  - k-bit Output Feedback Mode (OFB)

69

## Electronic Codebook (ECB)

- Consist of doing the obvious thing, and it is usually the worst method.. ;)
- The message is broke into 64-bit blocks, with padding for the last one
- Each block is independently encrypted with the secret key
  - $C_i = \text{DES}_{K_1}(P_i)$
  - each block is a value which is substituted, like a codebook



70

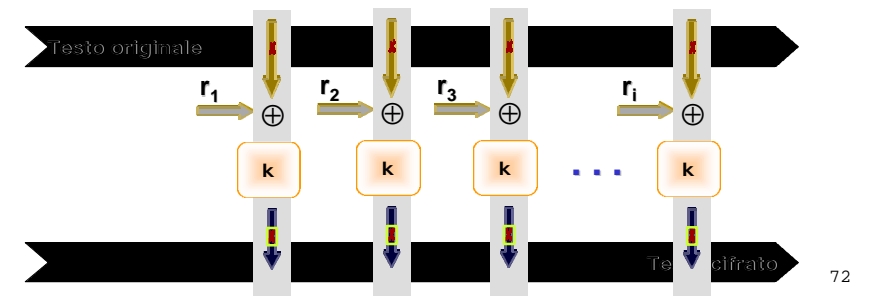
## Advantages and Limitations of ECB

- At end of message, handle possible last short block
  - by padding either with known non-data value (eg nulls)
  - or pad last block with count of pad size
    - eg. [ b1 b2 b3 0 0 0 5 ] <- 3 data bytes, then 5 bytes pad+count
- There are a number of problem that arise and that don't show up in the single block case
  - Repetitions in message may show in ciphertext if aligned with message block
  - if a message contains 2 identical 64-bit blocks, the corresponding cipher blocs are identical; it can be a problem
    - in some cases it can be possible to guess a portion of the message
    - in some cases it can be possible to alter the message
- As result, ECB is rarely used
  - main use is sending a few blocks of data

71

## Cipher Block Chaining (CBC)

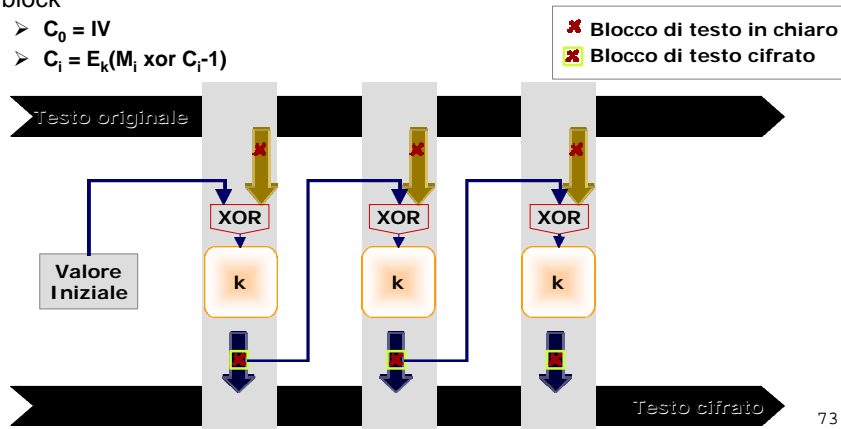
- CBC avoids some problems in ECB
- If the same block repeats in the plain text, it will not cause repeats of ciphertext
- Adds a feedback mechanism to the cipher
- Plaintext is more difficult to manipulate
- Basic idea:



72

## Cipher Block Chaining (CBC)

- Plaintext patterns are concealed by XORing this block of M with the previous block of C
- Requires an IV (Initialization vector) of random data to encrypt the first block
  - $C_0 = IV$
  - $C_i = E_k(M_i \text{ xor } C_{i-1})$



73

## Advantages and Limitations of CBC

- Decryption is simple because  $\oplus$  is reversible
- CBC has the same performance of ECB, except for the cost of generating and transmitting the IV
- Each ciphertext block depends on **all** message blocks
  - **thus a change in the message affects all ciphertext blocks after the change as well as the original block**
- It can be used the value of 0 as IV, however it can lead to some problems
  - **e.g. if a message is transmitted weekly, it is possible to guess if changes occurred**
  - **Moreover, IV!=0 prevents attackers for supplying chosen plaintext**
- If IV is sent in the clear, an attacker can change bits of the first block, and change IV to compensate
  - **hence either IV must be a fixed value (as in EFTPOS) or it must be sent encrypted in ECB mode before rest of message**

74

## CBC Threat 1 - Modifying ciphertext blocks

- Using CBC does not eliminate the problem of someone modifying the message in transit
- If the attacker changes the ciphertext block  $c_n$ ,  $c_n$  gets  $\oplus$ 'd with the decrypted  $c_{n+1}$  to yield  $m_{n+1}$ 
  - **changing bit h of  $c_n$  has predictable effect to bit h of  $m_{n+1}$**
  - **the attacker cannot know the new  $m_n$  (a new random 64-bit value, as side effect)**
- This threat can be combated by adding a CRC to the plaintext before encrypt

75

## CBC Threat 2 - Rearranging ciphertext blocks

- Knowing the plain text, the corresponding ciphertext and IV, it is possible to rearrange the  $c_1, c_2, c_3, \dots$  (building blocks), in such a way to obtain a new  $m_1, m_2, m_3 \dots$
- A CRC can help but not solve the problem (1 in  $2^{32}$  chance that the CRC will work; if the attack consist only in modifying the message, it is possible to try several combination)

76

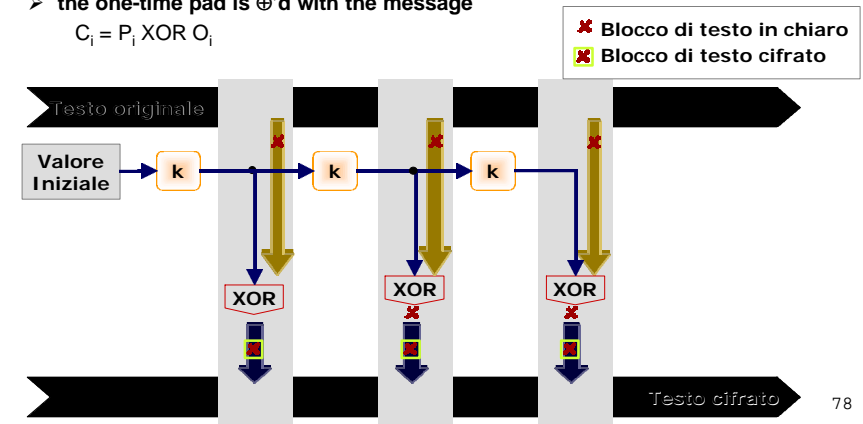
## Output Feedback (OFB)

- Acts like a pseudorandom number generator
- The message is encrypted by  $\oplus$ ing it with the pseudorandom stream generated by the OFB
  - message is treated as a stream of bits
- How it works:
  - A pseudorandom number  $O_0$  is generated (named IV as in CBC)
  - $O_0$  is encrypted (using secret key  $K$ ) obtaining  $O_1$
  - from  $O_1$  is obtained  $O_2$  and so on, as many block are needed
    - $O_i = E_K(O_{i-1})$
    - $O_0 = IV$
  - feedback is independent of message and can be computed in advance
  - so, a long pseudorandom string is generated (one-time pad)
  - the one-time pad is simply  $\oplus$ 'd with the message
    - $C_i = P_i \text{ XOR } O_i$
- Uses: stream encryption over noisy channels

77

## Output Feedback (OFB)

- OFB in short:
  - a long pseudorandom string is generated (one-time pad)
    - $O_i = E_K(O_{i-1})$
    - $O_0 = IV$
  - the one-time pad is  $\oplus$ 'd with the message
    - $C_i = P_i \text{ XOR } O_i$



78

## Advantages and Limitations of OFB

- Advantages of OFB:
  - one-time pad can be generated in advances
  - if some bits of the ciphertext get garbled, only those bits of plaintext get garbled (no error propagation)
  - if a message arrives in arbitrary-sized chunks, the associated ciphertext can immediately be transmitted
- Disadvantages of OFB:
  - sender and receiver must remain in sync, and some recovery method is needed to ensure this occurs
  - if the plaintext and the ciphertext is known by a bad guy, he can modify the plaintext into anything he wants
  - hence must never reuse the same sequence (key+IV)

79

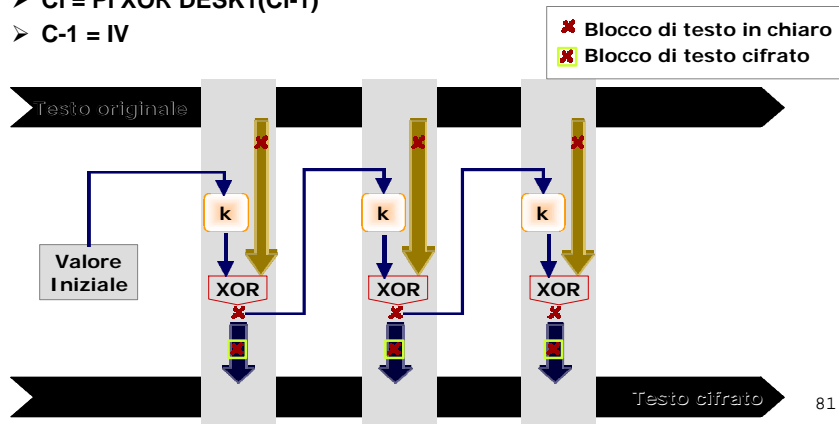
## Cipher FeedBack (CFB)

- Very similar to OFB
- The  $k$ -bit shifted in to the encryption module are the  $k$ -bit of the ciphertext from the previous block
- added to the output of the block cipher
- result is feed back for next stage (hence name)
  - $C_i = P_i \text{ XOR } \text{DES}_{K1}(C_{i-1})$
  - $C_{-1} = IV$

80

## Cipher Feedback (CFB)

- Very similar to OFB
- The k-bit shifted in to the encryption module are the k-bit of the ciphertext from the previous block
  - $C_i = P_i \text{ XOR } \text{DESK}_1(C_{i-1})$
  - $C_{-1} = \text{IV}$



81

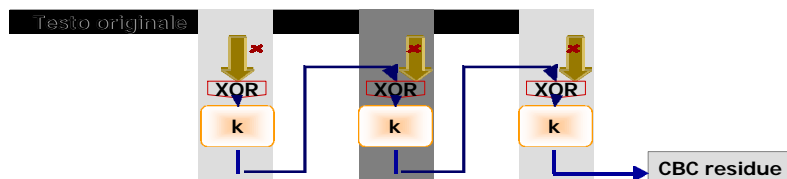
## Advantages and Limitations of CFB

- Note: the block cipher is used in **encryption** mode at **both** ends
- The one-time pad cannot be generated in CFB
- Limitation is need to stall while do block encryption after every n-bits
- Errors propagate for several blocks after the error
- it is possible to have k-bit CFB with k different from 64 (e.g. 8)
  - With OFB or CBC if character are lost in transmission or extra character are added, the rest of trasmission is garbled
  - With 8-bit CFB as long as an error is an integral number of bytes, things will be resynchronized
    - a disadvantage is that DES operation is required each byte

82

## Integrity: Generating MICs

- CBC, CFB and OFB, when properly used, offer good protection against an eavesdropper deciphering a message
- None of these offers good protection against an eavesdropper (who already knows the plaintext or not) modifying it undetected
  - note that any random string of bits will decrypt into something)
- In many context message are not secret but integrity must be assured
- A secret key system can be used to generate a cryptographic checksum known as MIC (Message Integrity Code)
- A standard way of protection is to compute the CBC but send only the last block (named CBC residue) along with the plaintext



83

## Ensuring Privacy and Integrity

- To assure privacy it is possible to CBC-encrypt the message
- To assure integrity is appropriate to transmit unencrypted data plus a CBC residue
- To assure both privacy and integrity, is not sufficient to CBC-encrypt the message, nor sending together a CBC-residue
- A possible solution is to send CBC-encrypted message with a CBC-residue, computed with two different keys
  - **double complexity!**

84

## Ensuring Privacy and Integrity

- Other possible solutions:
  - **CBC with a weak cryptography checksum**
    - e.g. Kerberos V4
  - **CBC with cryptography hash**
    - two cryptographic computations such as CBC with two different keys, but more efficient (thanks to hash algorithms)
      - e.g. with MD4, MD5, etc
  - **CBC encryption and CBC residue with related keys**
    - it could be sufficient to switch just one bit
      - e.g. kerberos V5  $\oplus$ s the key with 0xF0F0F0F0F0F0F0
      - this has the property of preserving key parity and never transforming non-weak key into a weak-key